

# **Summative Blueprints for Mathematics**

#### **General Information**

Each of the following blueprints is for a summative Mathematics assessment in grades 3 through 9. Each assessment follows a linear design (also referred to as fixed) for Spring 2022. It is estimated to take about two hours for students to complete.

Each Math item measures either the content defined by the standard or the practice of argumentation or modeling. Each content item is worth 1 point and is machine scored. Item types include multiple choice, other selected response, and constructed response. Argumentation and modeling items are either human scored or machine scored. The machine-scored items are worth 1, 2, or 3 points and include the same item types as the content items. The human-scored items include at least one extended-response part with an embedded equation editor.

The grade-level blueprints that follow provide more detailed information about the measurement of knowledge and skills in each content category within a form, including the percentage and number of points allocated to each content category.



A grade 3 test form will include a total of 50 points distributed in the three task types: content, argumentation, and modeling.

Each form will include 40 machine-scored content items, each worth 1 point. Item types will include multiple choice, other selected response, and constructed response. Each item will be aligned to at least one of the standards within a content category in the following table.

Each form will include a total of 5 points from argumentation items. One item will be a humanscored constructed-response item worth 3 points. Each argumentation item is aligned to one content standard and one or more of the Standards for Mathematical Practice.

Each form will include a total of 5 points from modeling items. One item will be a human-scored constructed-response item worth 3 points. Each modeling item is aligned to one content standard and one or more of the Standards for Mathematical Practice.

| Claim                      | Content Category                  | Weight Within<br>Form* | Points |  |
|----------------------------|-----------------------------------|------------------------|--------|--|
|                            | Operations and Algebraic Thinking | 28%                    | 14     |  |
|                            | Numbers and Operations in Base 10 | 20%                    | 10     |  |
| Content                    | Numbers and Operations–Fractions  | 20%                    |        |  |
|                            | Measurement and Data              | 24%                    | 12     |  |
|                            | Geometry                          | 8%                     | 4      |  |
| Content                    |                                   |                        | 40     |  |
| Argumentation              | ANY                               | 10%                    | 5      |  |
| Modeling                   | ANY 10%                           |                        | 5      |  |
| Argumentation and Modeling |                                   |                        | 10     |  |
| Total Points               |                                   |                        | 50     |  |

<sup>\*</sup>Some percentages have been rounded up to the next whole number, which may result in a total higher than 100.



A grade 4 test form will include a total of 50 points distributed in the three task types: content, argumentation, and modeling.

Each form will include 40 machine-scored content items, each worth 1 point. Item types will include multiple choice, other selected response, and constructed response. Each item will be aligned to at least one of the standards within a content category in the following table.

Each form will include a total of 5 points from argumentation items. One item will be a humanscored constructed-response item worth 3 points. Each argumentation item is aligned to one content standard and one or more of the Standards for Mathematical Practice.

Each form will include a total of 5 points from modeling items. One item will be a human-scored constructed-response item worth 3 points. Each modeling item is aligned to one content standard and one or more of the Standards for Mathematical Practice.

| Claim                      | Content Category                  | Weight Within<br>Form* | Points |  |
|----------------------------|-----------------------------------|------------------------|--------|--|
|                            | Operations and Algebraic Thinking | 12%                    | 6      |  |
|                            | Numbers and Operations in Base 10 | 36%                    | 18     |  |
| Content                    | Numbers and Operations–Fractions  | 30 /0                  | 10     |  |
|                            | Measurement and Data              | 16%                    | 8      |  |
|                            | Geometry                          | 16%                    | 8      |  |
| Content                    |                                   |                        | 40     |  |
| Argumentation              | ANY                               | 10%                    | 5      |  |
| Modeling                   | ANY                               | 5                      |        |  |
| Argumentation and Modeling |                                   |                        | 10     |  |
| <b>Total Points</b>        |                                   |                        | 50     |  |

<sup>\*</sup>Some percentages have been rounded up to the next whole number, which may result in a total higher than 100.



A grade 5 test form will include a total of 50 points distributed in the three task types: content, argumentation, and modeling.

Each form will include 40 machine-scored content items, each worth 1 point. Item types will include multiple choice, other selected response, and constructed response. Each item will be aligned to at least one of the standards within a content category in the following table.

Each form will include a total of 5 points from argumentation items. One item will be a human-scored constructed-response item worth 3 points. Each argumentation item is aligned to one content standard and one or more of the Standards for Mathematical Practice.

Each form will include a total of 5 points from modeling items. One item will be a human-scored constructed-response item worth 3 points. Each modeling item is aligned to one content standard and one or more of the Standards for Mathematical Practice.

| Claim               | Content Category                     | Weight Within<br>Form* | Points |  |
|---------------------|--------------------------------------|------------------------|--------|--|
|                     | Operations and Algebraic Thinking 8% |                        | 4      |  |
|                     | Numbers and Operations in Base 10    | 40%                    | 20     |  |
| Content             | Numbers and Operations–Fractions     | 40 /0                  | 20     |  |
|                     | Measurement and Data 20%             |                        | 10     |  |
|                     | Geometry                             | 12%                    | 6      |  |
| Content             |                                      |                        | 40     |  |
| Argumentation       | ANY                                  | 10%                    | 5      |  |
| Modeling            | ANY                                  | 5                      |        |  |
| Argumentation       |                                      |                        | 10     |  |
| and Modeling        |                                      |                        | 10     |  |
| <b>Total Points</b> |                                      |                        | 50     |  |

<sup>\*</sup>Some percentages have been rounded up to the next whole number, which may result in a total higher than 100.



A grade 6 test form will include a total of 57 points distributed in the three task types: content, argumentation, and modeling.

Each form will include 45 machine-scored content items, each worth 1 point. Item types will include multiple choice, other selected response, and constructed response. Each item will be aligned to at least one of the standards within a content category in the following table.

Each form will include a total of 6 points from argumentation items. One item will be a humanscored constructed-response item worth 4 points. Each argumentation item is aligned to one content standard and one or more of the Standards for Mathematical Practice.

Each form will include a total of 6 points from modeling items. One item will be a human-scored constructed-response item worth 4 points. Each modeling item is aligned to one content standard and one or more of the Standards for Mathematical Practice.

| Claim               | Content Category  Weight Within Form* |     | Points |
|---------------------|---------------------------------------|-----|--------|
|                     | Ratio and Proportion                  | 18% | 10     |
|                     | The Number System                     | 18% | 10     |
| Content             | Expression and Equations              | 19% | 11     |
|                     | Geometry                              | 12% | 7      |
|                     | Statistics and Probability            | 12% | 7      |
| Content             |                                       |     | 45     |
| Argumentation       | ANY                                   | 11% | 6      |
| Modeling            | ANY                                   | 6   |        |
| Argumentation       |                                       |     | 12     |
| and Modeling        |                                       |     | 12     |
| <b>Total Points</b> |                                       |     | 57     |

<sup>\*</sup>Some percentages have been rounded up to the next whole number, which may result in a total higher than 100.



A grade 7 test form will include a total of 57 points distributed in the three task types: content, argumentation, and modeling.

Each form will include 45 machine-scored content items, each worth 1 point. Item types will include multiple choice, other selected response, and constructed response. Each item will be aligned to at least one of the standards within a content category in the following table.

Each form will include a total of 6 points from argumentation items. One item will be a humanscored constructed-response item worth 4 points. Each argumentation item is aligned to one content standard and one or more of the Standards for Mathematical Practice.

Each form will include a total of 6 points from modeling items. One item will be a human-scored constructed-response item worth 4 points. Each modeling item is aligned to one content standard and one or more of the Standards for Mathematical Practice.

| Claim                      | Content Category           | Weight Within<br>Form* | Points |  |
|----------------------------|----------------------------|------------------------|--------|--|
|                            | Ratio and Proportion       | 16%                    | 9      |  |
|                            | The Number System          | 12%                    | 7      |  |
| Content                    | Expression and Equations   | 19%                    | 11     |  |
|                            | Geometry                   | 16%                    | 9      |  |
|                            | Statistics and Probability | 16%                    | 9      |  |
| Content                    |                            |                        | 45     |  |
| Argumentation              | ANY                        | 11%                    | 6      |  |
| Modeling                   | ANY                        | 6                      |        |  |
| Argumentation and Modeling |                            |                        | 12     |  |
| Total Points               |                            |                        | 57     |  |

<sup>\*</sup>Some percentages have been rounded up to the next whole number, which may result in a total higher than 100.



A grade 8 test form will include a total of 57 points distributed in the three task types: content, argumentation, and modeling.

Each form will include 45 machine-scored content items, each worth 1 point. Item types will include multiple choice, other selected response, and constructed response. Each item will be aligned to at least one of the standards within a content category in the following table.

Each form will include a total of 6 points from argumentation items. One item will be a humanscored constructed-response item worth 4 points. Each argumentation item is aligned to one content standard and one or more of the Standards for Mathematical Practice.

Each form will include a total of 6 points from modeling items. One item will be a human-scored constructed-response item worth 4 points. Each modeling item is aligned to one content standard and one or more of the Standards for Mathematical Practice.

| Claim                      | Content Category Weight Within Form* |     | Points |
|----------------------------|--------------------------------------|-----|--------|
|                            | The Number System                    | 2%  | 1      |
|                            | Expression and Equations             | 23% | 13     |
| Content                    | Functions                            | 25% | 14     |
|                            | Geometry                             | 19% | 11     |
|                            | Statistics and Probability           | 11% | 6      |
| Content                    |                                      |     | 45     |
| Argumentation              | ANY                                  | 11% | 6      |
| Modeling                   | ANY 11%                              |     | 6      |
| Argumentation and Modeling |                                      | •   | 12     |
| <b>Total Points</b>        |                                      |     | 57     |

<sup>\*</sup>Some percentages have been rounded up to the next whole number, which may result in a total higher than 100.



A grade 9 test form will include a total of 68 points distributed in the three task types: content, argumentation, and modeling.

Each form will include 48 machine-scored content items, each worth 1 point. Item types will include multiple choice, other selected response, and constructed response. Each item will be aligned to at least one of the standards within a content category in the following table.

Each form will include a total of 10 points from argumentation items. One item will be a humanscored constructed-response item worth 4 points. Each argumentation item is aligned to one content standard and one or more of the Standards for Mathematical Practice.

Each form will include a total of 10 points from modeling items. One item will be a human-scored constructed-response item worth 4 points. Each modeling item is aligned to one content standard and one or more of the Standards for Mathematical Practice.

| Claim                      | Content Category           | Weight Within<br>Form* | Points |
|----------------------------|----------------------------|------------------------|--------|
|                            | Number and Quantity        | 7%                     | 5      |
| Content                    | Algebra                    | 28%                    | 19     |
| Content                    | Functions                  | 28%                    | 19     |
|                            | Statistics and Probability | 7%                     | 5      |
| Content                    |                            |                        | 48     |
| Argumentation              | ANY                        | 15%                    | 10     |
| Modeling                   | ANY                        | 15%                    | 10     |
| Argumentation and Modeling |                            |                        | 20     |
| <b>Total Points</b>        |                            |                        | 68     |

<sup>\*</sup>Some percentages have been rounded up to the next whole number, which may result in a total higher than 100.



# Summary of Points by Grade

| Claim         | Content<br>Category   | Grade<br>3 | Grade<br>4 | Grade<br>5 | Grade<br>6 | Grade<br>7 | Grade<br>8 | Grade<br>9 |
|---------------|---|------------|------------|------------|------------|------------|------------|------------|
|               | Operations and<br>Algebraic<br>Thinking                             | 14         | 6          | 4          | n/a        | n/a        | n/a        | n/a        |
|               | Numbers and Operations in Base 10 Numbers and Operations— Fractions | 10         | 18         | 20         | n/a        | n/a        | n/a        | n/a        |
|               | Measurement<br>and Data   | 12         | 8          | 10         | n/a        | n/a        | n/a        | n/a        |
| Content       | Geometry  | 4          | 8          | 6          | 7          | 9          | 11         | n/a        |
|               | Ratio and<br>Proportion   | n/a        | n/a        | n/a        | 10         | 9          | n/a        | n/a        |
|               | The Number<br>System  | n/a        | n/a        | n/a        | 10         | 7          | 1          | n/a        |
|               | Expression and<br>Equations   | n/a        | n/a        | n/a        | 11         | 11         | 13         | n/a        |
|               | Statistics and<br>Probability                                       | n/a        | n/a        | n/a        | 7          | 9          | 6          | 5          |
|               | Functions   | n/a        | n/a        | n/a        | n/a        | n/a        | 14         | 19         |
|               | Number and<br>Quantity  | n/a        | n/a        | n/a        | n/a        | n/a        | n/a        | 5          |
|               | Algebra   | n/a        | n/a        | n/a        | n/a        | n/a        | n/a        | 19         |
| Argumentation | Argumentation   | 5          | 5          | 5          | 6          | 6          | 6          | 10         |
| and Modeling  | Modeling  | 5          | 5          | 5          | 6          | 6          | 6          | 10         |
| TOTAL         |   | 50         | 50         | 50         | 57         | 57         | 57         | 68         |